

# Learning From Interpretation Transitions

## - LFIT 2024 Summary -

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Independent Researcher

18th April 2024, LS2N, Nantes

# Outline

1 LFIT Overview

2 LFIT Story

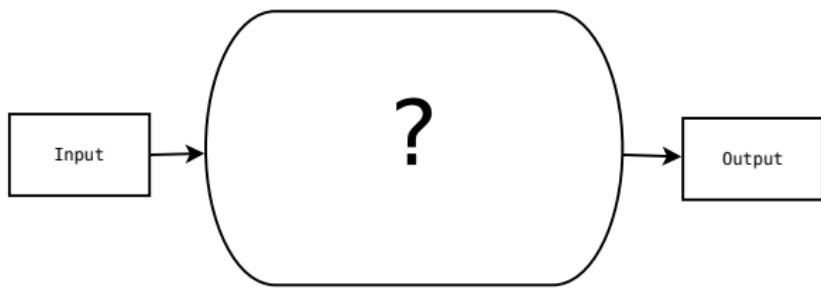
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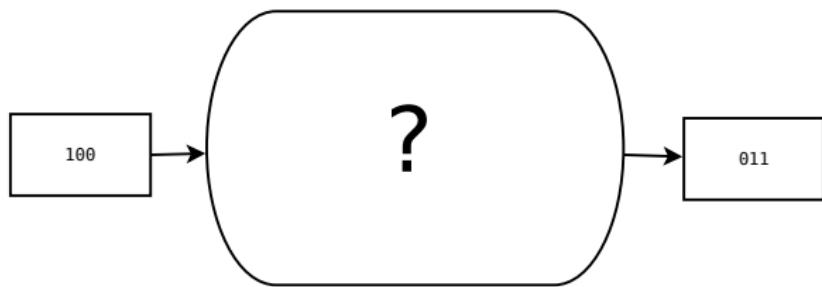
# Learning From Interpretation Transitions

**Idea:** given a set of **input/output** states of a **black-box** system, learn its **internal mechanics**.



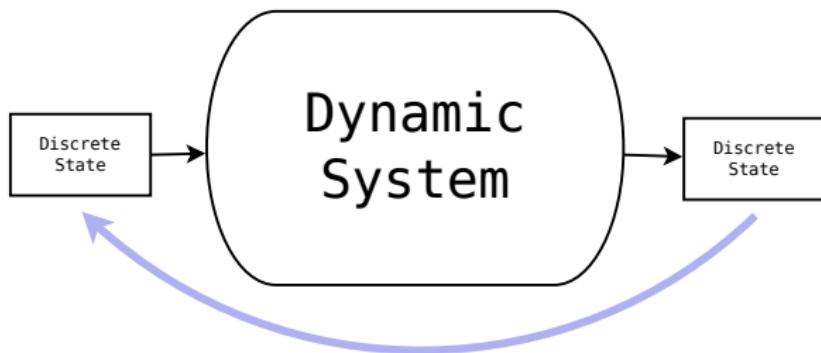
# Learning From Interpretation Transitions

**Discrete system:** input/output are vectors of **same size** which contain discrete values.



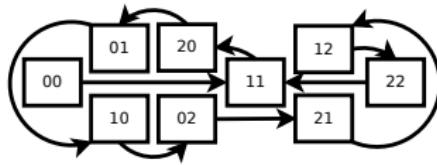
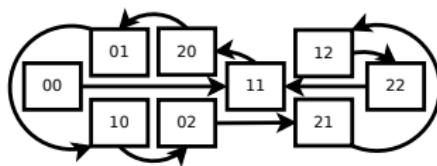
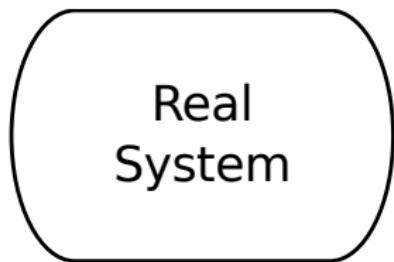
# Learning From Interpretation Transitions

**Dynamic system:** input/output are states of the system and **output** becomes the **next input**.



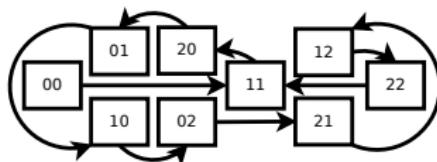
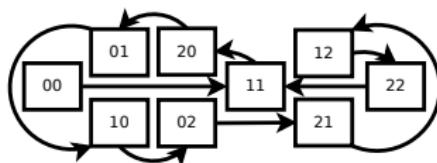
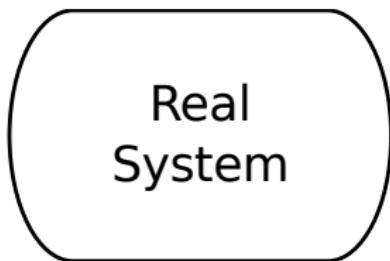
# Learning From Interpretation Transitions

**Goal:** produce an **artificial system** with the **same behavior** as the one observed, i.e., a **digital twin**.



# Learning From Interpretation Transitions

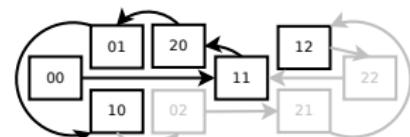
**Representation:** propositional logic programs with annotated atoms encoding multi-valued variables.



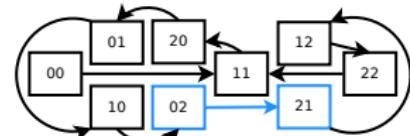
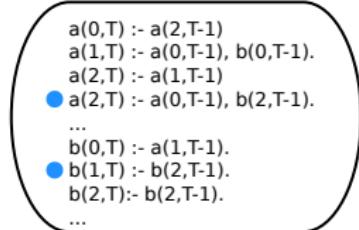
# Learning From Interpretation Transitions

**Method:** learn the dynamics of systems from the observations of some of its state transitions.

DATA



RESULTS

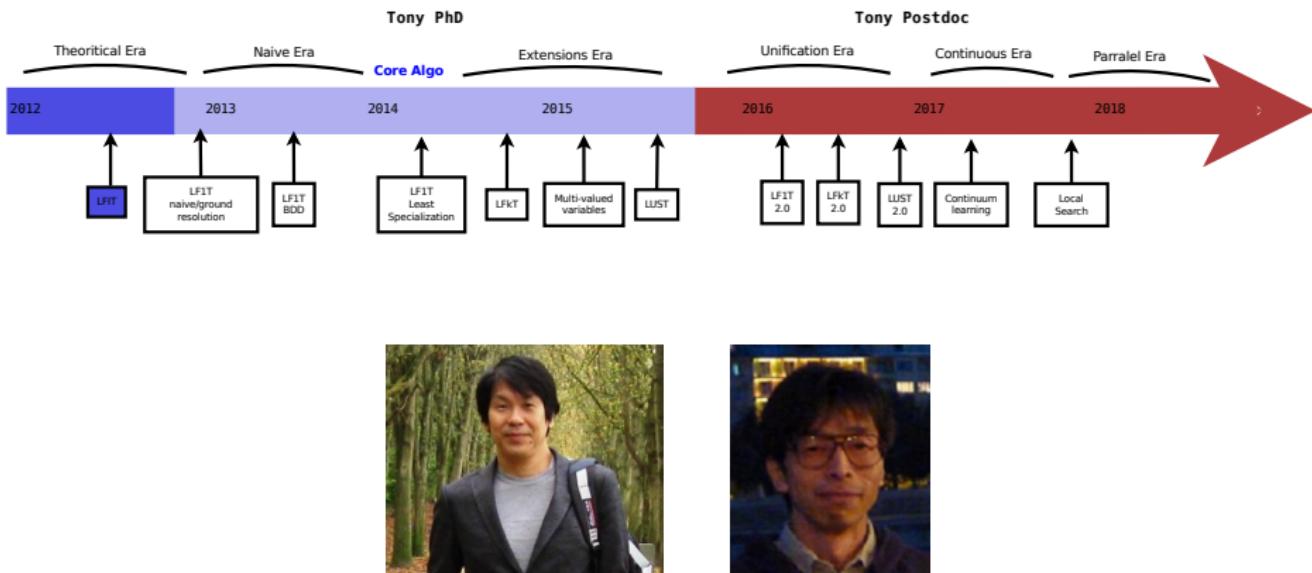


# Outline

1 LFIT Overview

2 LFIT Story

# LFIT Chronology



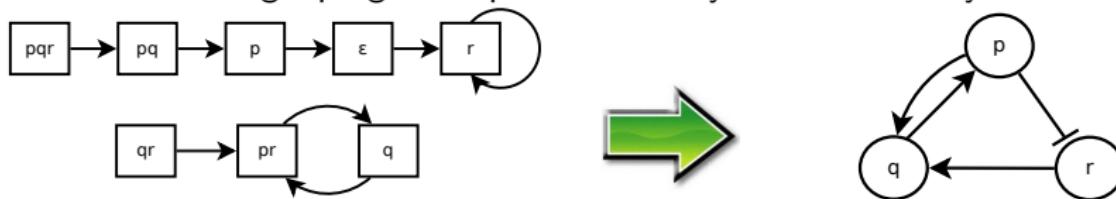
Short paper **ILP 2012.**

# Learning From Interpretation Transitions (LFIT)

A framework for learning system dynamics from state transitions.

- **Basic Idea:**

- ▶ Learn a logic program by observing the behavior of a system.
- ▶ This logic program represents the dynamics of the system.



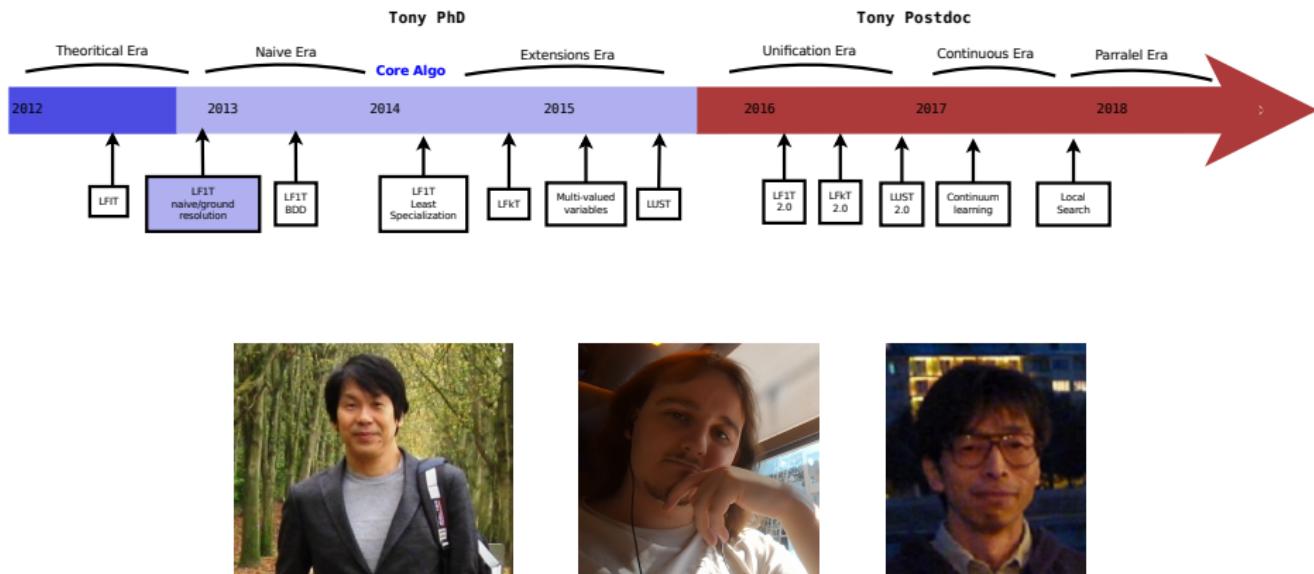
**Input:** Behavior of the system

**Output:** Dynamics of the system

$$\begin{aligned}
 p(t+1) &\leftarrow q(t). \\
 q(t+1) &\leftarrow p(t) \wedge r(t). \\
 r(t+1) &\leftarrow \neg p(t).
 \end{aligned}$$

**Representation:** Logic Program

# LFIT Chronology

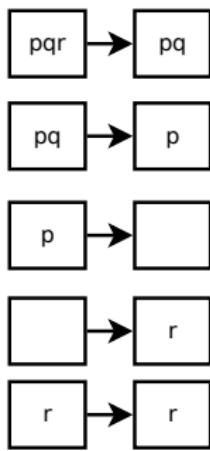


Long paper ILP 2013/2014, journal MLJ 2014.

# LFIT: Learning From 1-step Transitions (memory-less Boolean systems)

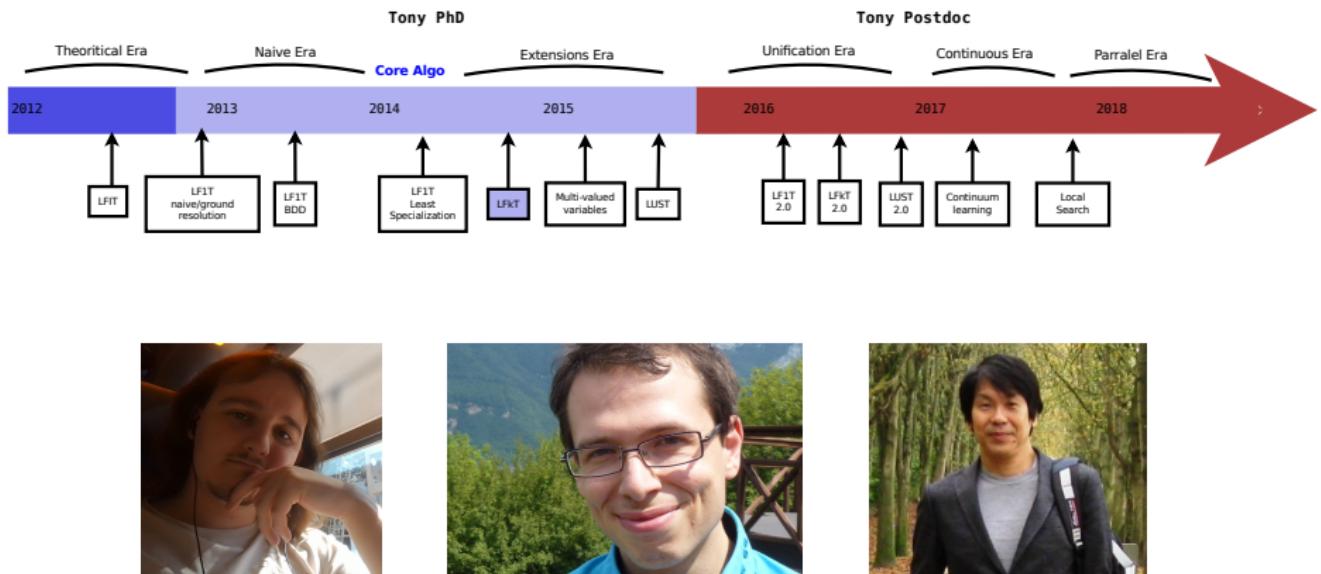
**INPUT:**  
A set of pairs of interpretations

**OUTPUT:**  
A normal logic program



$p(t+1) \leftarrow q(t).$   
 $q(t+1) \leftarrow p(t) \wedge r(t).$   
 $r(t+1) \leftarrow \neg p(t).$

# LFIT Chronology

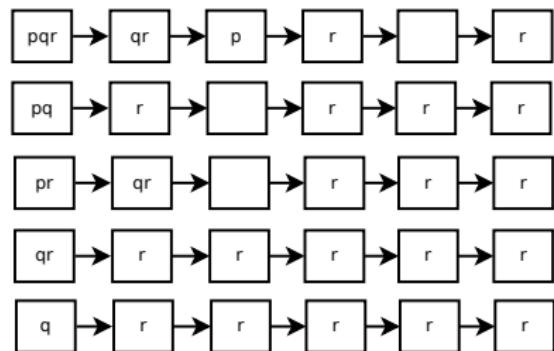


Short paper **ILP 2014/2015**, journal **Frontiers 2015**, long paper **ICMLA 2015**.

# LFkT: Learning From k-step Transitions (markov( $k$ ) Boolean systems)

**INPUT:**

A set of **sequences** of interpretations

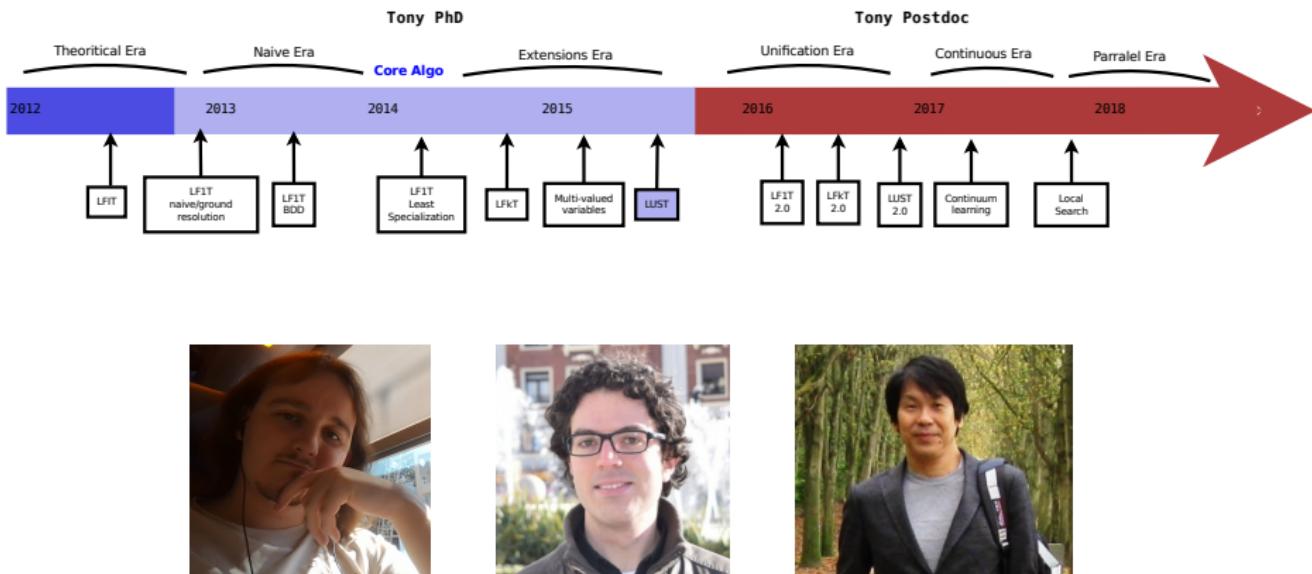


**OUTPUT:**

A normal logic program  
with delay

$$\begin{aligned}
 p(t) &\leftarrow q(t-1) \wedge q(t-2). \\
 q(t) &\leftarrow p(t-1) \wedge r(t-1). \\
 r(t) &\leftarrow \neg p(t-2).
 \end{aligned}$$

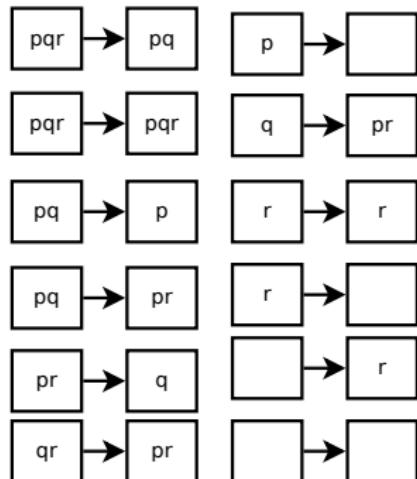
# LFIT Chronology



Tech. com ICLP 2015, long paper ICAPS 2016, journal JMLR 2017.

# LUST: Learning from Uncertain State Transitions (non-deterministic systems)

**INPUT:**  
A set of pairs of interpretations

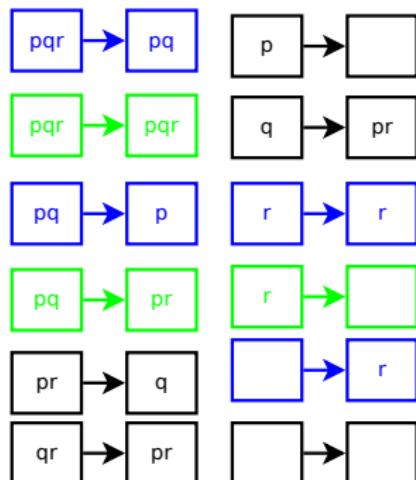


**OUTPUT:**  
A **set** of normal logic programs

$$\begin{aligned}
 & p(t) \leftarrow q(t-1). \\
 & q(t) \leftarrow p(t-1) \wedge r(t-1). \\
 & \textcolor{blue}{r(t) \leftarrow \neg p(t-1).} \\
 & \oplus \\
 & p(t) \leftarrow q(t-1). \\
 & q(t) \leftarrow p(t-1) \wedge r(t-1). \\
 & \textcolor{green}{r(t) \leftarrow q(t-1).}
 \end{aligned}$$

# LUST: Learning from Uncertain State Transitions (non-deterministic systems)

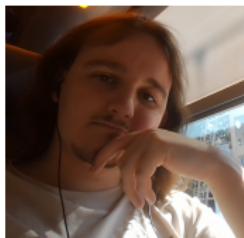
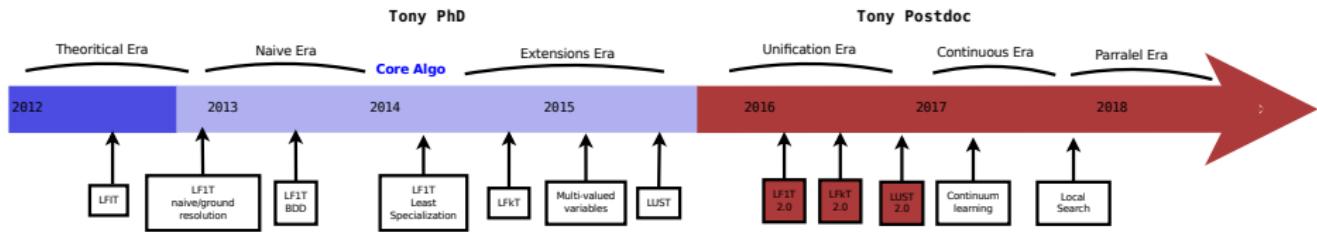
**INPUT:**  
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**OUTPUT:**  
A **set** of normal logic programs

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# LFIT Chronology



# Motivation: biological system modeling

## Projects

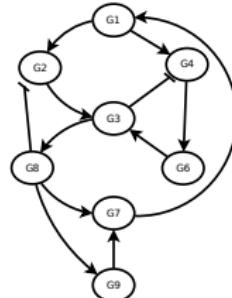
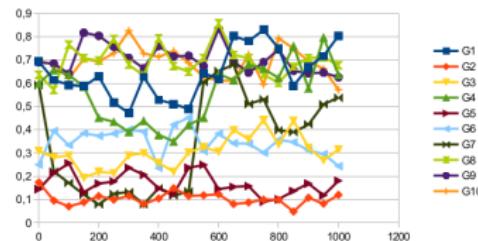
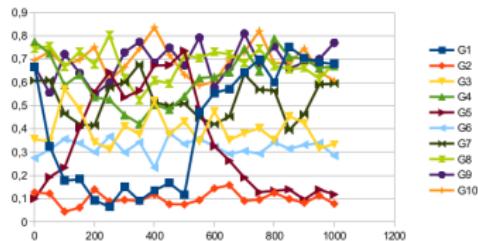
- Hyclock: influences modeling
- DREAM Challenge 11: predictions
- Biology Institute of Valrose: gene level of expression

# Hyclock project: modeling the mammalian circadian clock

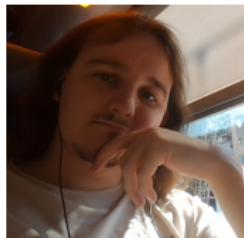
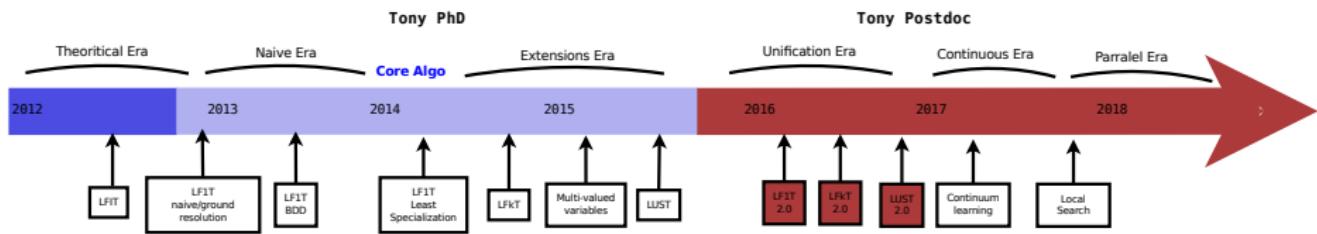
## Data

- 45,000 variables
- 2 time series of 30h
- 1 data point per hour for each variable

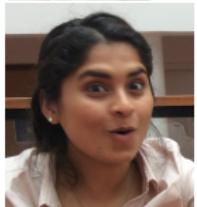
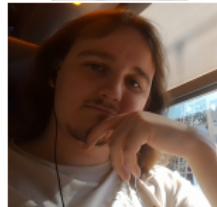
Goal: extract gene influences



# LFIT Chronology



# DREAM Challenge 11: Team



3 Professors: Olivier Roux, Paco Chinesta, Katsumi Inoue

2 Associate Professors: Morgan Magnin and Carito Guziolowski

2 Postdocs: Tony Ribeiro and Domenico Borzachiello

3 PhD: Bertrand Miannay, Emna Ben Abdallah, Misbah Razzak

# DREAM Challenge 11: competition

## Data

- 120 patients, 7 viruses
- Time series over 22 000 variables (gene probes)
- Meta data: shedding, symptomatic and symptoms

## Specificities

- Irregular time points over 240h
- Different sizes of the series

## Challenge

- 25 test patients
- Subchallenge 1: predict probability of shedding
- Subchallenge 2: predict probability of symptomatic
- Subchallenge 3: predict logsymptoms

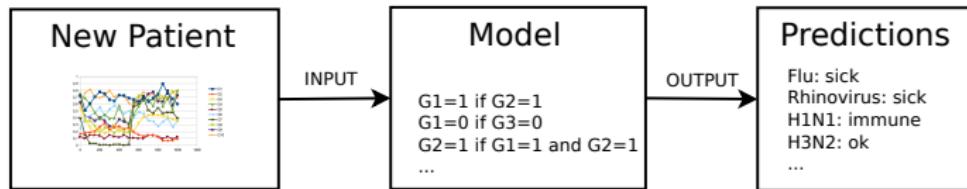
# DREAM Challenge 11: competition

## Data

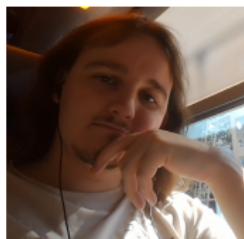
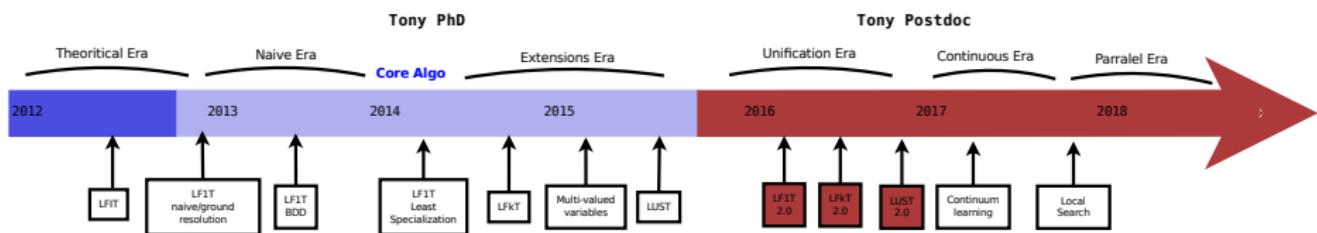
- 120 patients, 7 viruses
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- Meta data: shedding, symptomatic and symptoms

## Specificities

- Irregular time points over 240h
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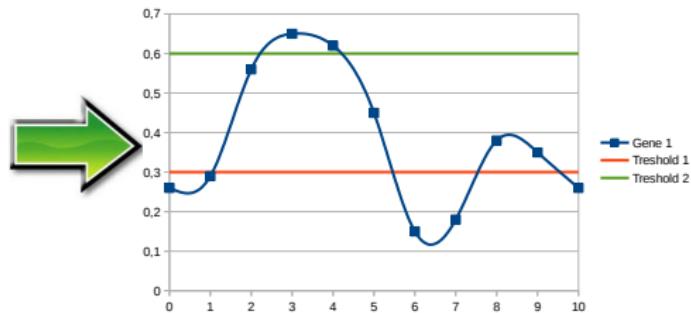
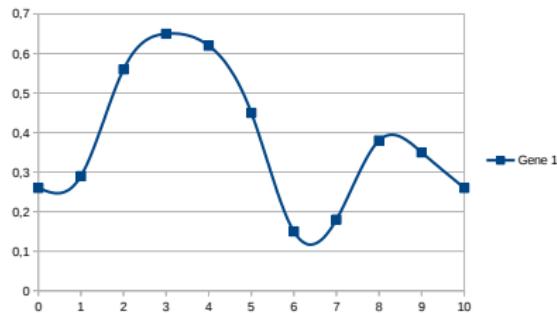


# Identification of gene level of expression

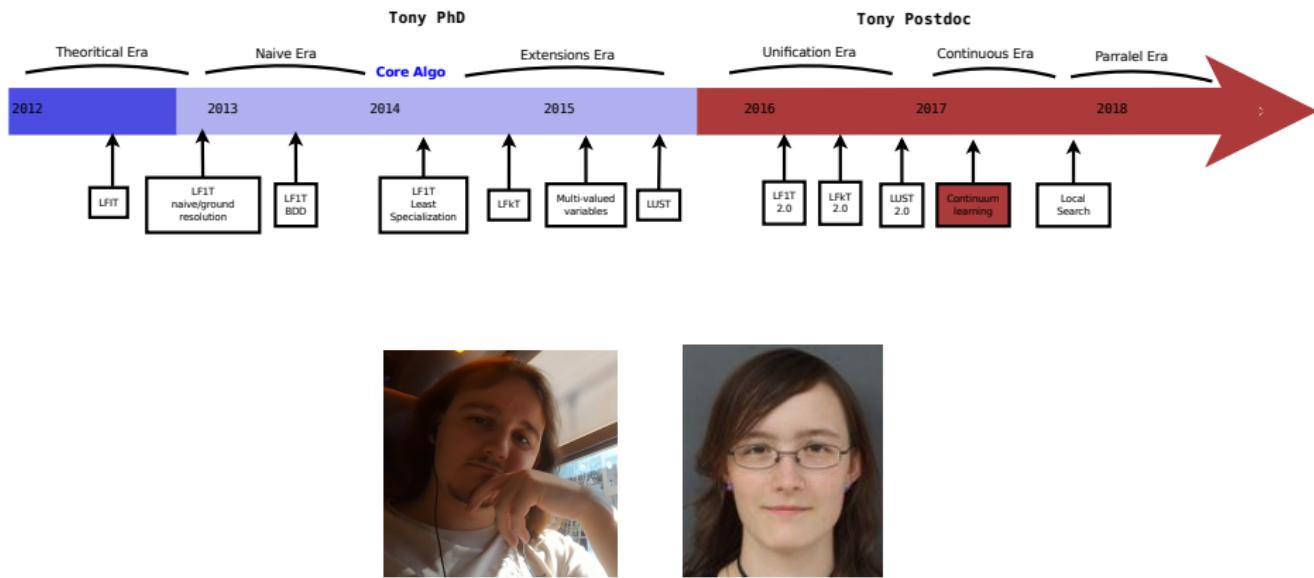
## Data

- 2 genes
- time series **on demand**
- precision **on demand**

Goal: extract the **levels of expression** of both gene

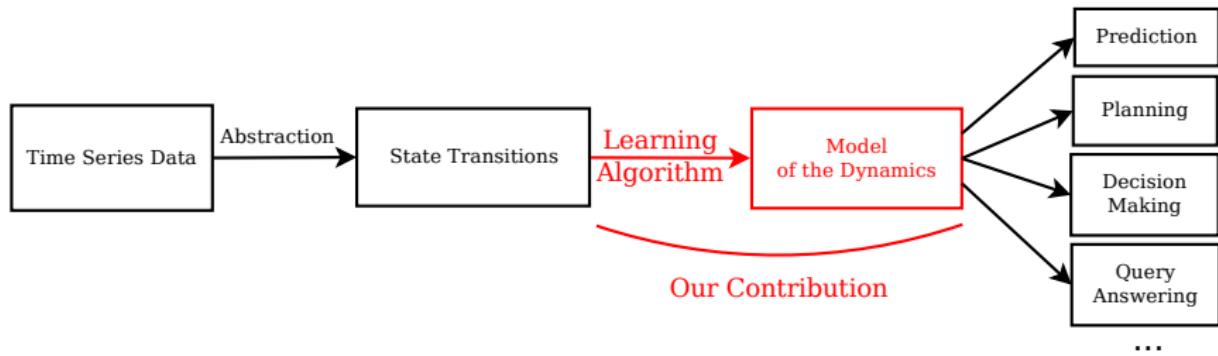


# LFIT Chronology

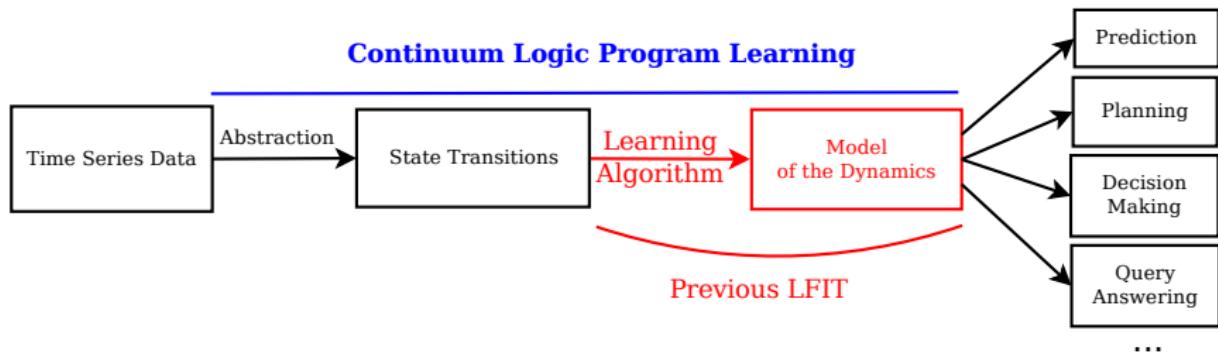


Long paper ILP 2017.

# LFIT process



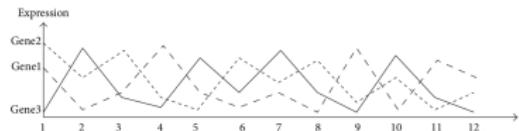
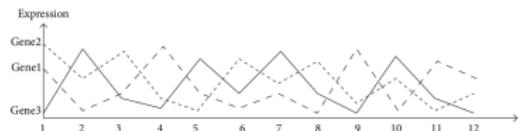
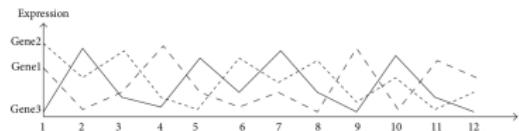
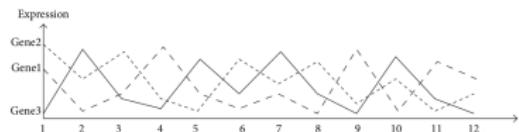
# LFIT process



# Continuum Logic Program

**INPUT:**

A set of **time series data**



**OUTPUT:**

A **continuum logic program**

$$p([0, 0.5], t) \leftarrow q([0, 0.5], t - 1).$$

$$p([0.5, 1], t) \leftarrow q([0.5, 1], t - 1).$$

$$q([0, 0.5], t) \leftarrow p([0, 0.5], t - 1) \wedge r([0.5, 1], t - 1).$$

$$q([0.5, 1], t) \leftarrow p([0.5, 1], t - 1) \wedge r([0.5, 1], t - 1).$$

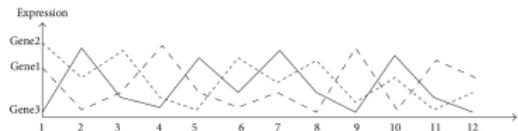
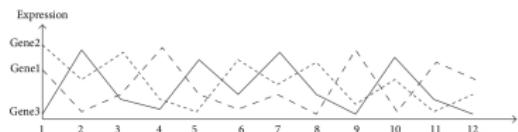
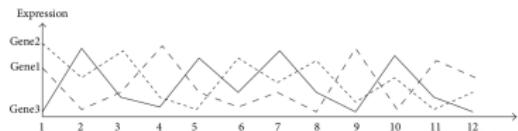
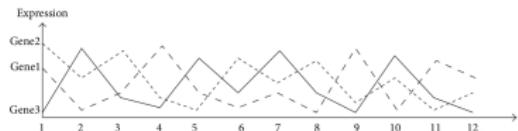
$$r([0, 0.5], t) \leftarrow p([0.5, 1], t - 1).$$

$$r([0.5, 1], t) \leftarrow p([0, 0.5], t - 1).$$

# Continuum Logic Program

**INPUT:**

A set of **time series data**



**OUTPUT:**

A **continuum logic program**

$$p([0, 0.5], t) \leftarrow q([0, 0.5], t - 1).$$

$$p([0.5, 1], t) \leftarrow q([0.5, 1], t - 1).$$

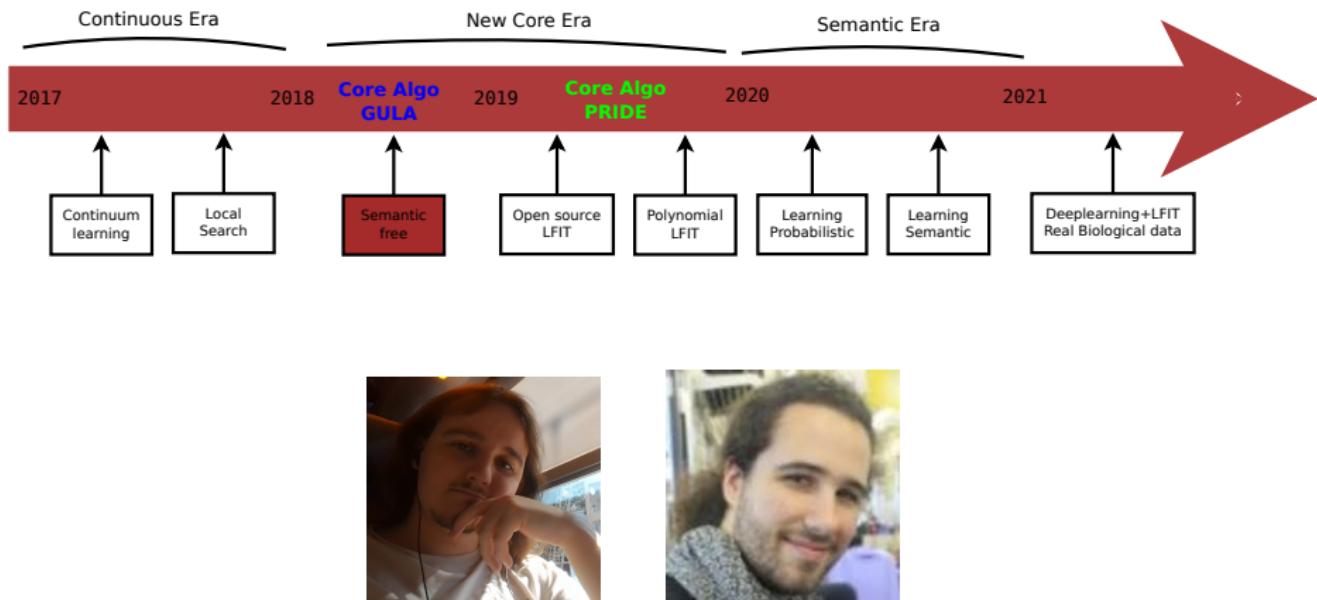
$$q([0, 0.5], t) \leftarrow p([0, 0.5], t - 1) \wedge r([0.32, 1], t - 1).$$

$$q([0.5, 1], t) \leftarrow p([0.5, 1], t - 1) \wedge r([0.32, 1], t - 1).$$

$$r([0, 0.32], t) \leftarrow p([0.5, 1], t - 1).$$

$$r([0.32, 1], t) \leftarrow p([0, 0.5], t - 1).$$

# LFIT Chronology



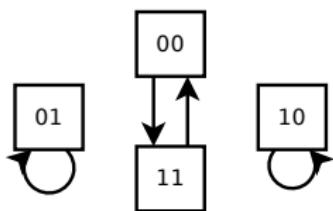
Long paper ILP 2018.

# Dynamical Semantics

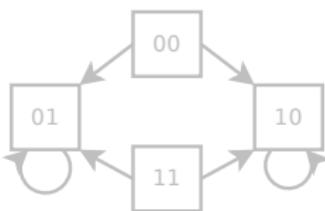
Boolean network transitions differ according to the update semantics used.



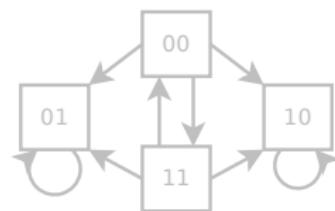
$$\begin{aligned} f(a) &:= \text{not } b. \\ f(b) &:= \text{not } a. \end{aligned}$$



Synchronous



Asynchronous



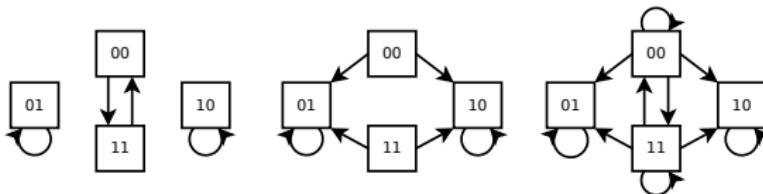
General

- Synchronous: all variables are updated
- Asynchronous: only one variable is updated
- General: any number of variables can be updated

# General Usage LFIT Algorithm (**GULA**) output



$f(a) := \text{not } b.$   
 $f(b) := \text{not } a.$



Synchronous

//  $f(a) := \text{not } b$   
 $a_t^0 \leftarrow b_{t-1}^1$   
 $a_t^1 \leftarrow b_{t-1}^0$

//  $f(b) := \text{not } a$   
 $b_t^0 \leftarrow a_{t-1}^1$   
 $b_t^1 \leftarrow a_{t-1}^0$

Asynchronous

//  $f(a) := \text{not } b$   
 $a_t^0 \leftarrow b_{t-1}^1$   
 $a_t^1 \leftarrow b_{t-1}^0$

//  $f(b) := \text{not } a$   
 $b_t^0 \leftarrow a_{t-1}^1$   
 $b_t^1 \leftarrow a_{t-1}^0$

General

//  $f(a) := \text{not } b$   
 $a_t^0 \leftarrow b_{t-1}^1$   
 $a_t^1 \leftarrow b_{t-1}^0$

//  $f(b) := \text{not } a$   
 $b_t^0 \leftarrow a_{t-1}^1$   
 $b_t^1 \leftarrow a_{t-1}^0$

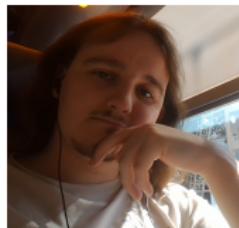
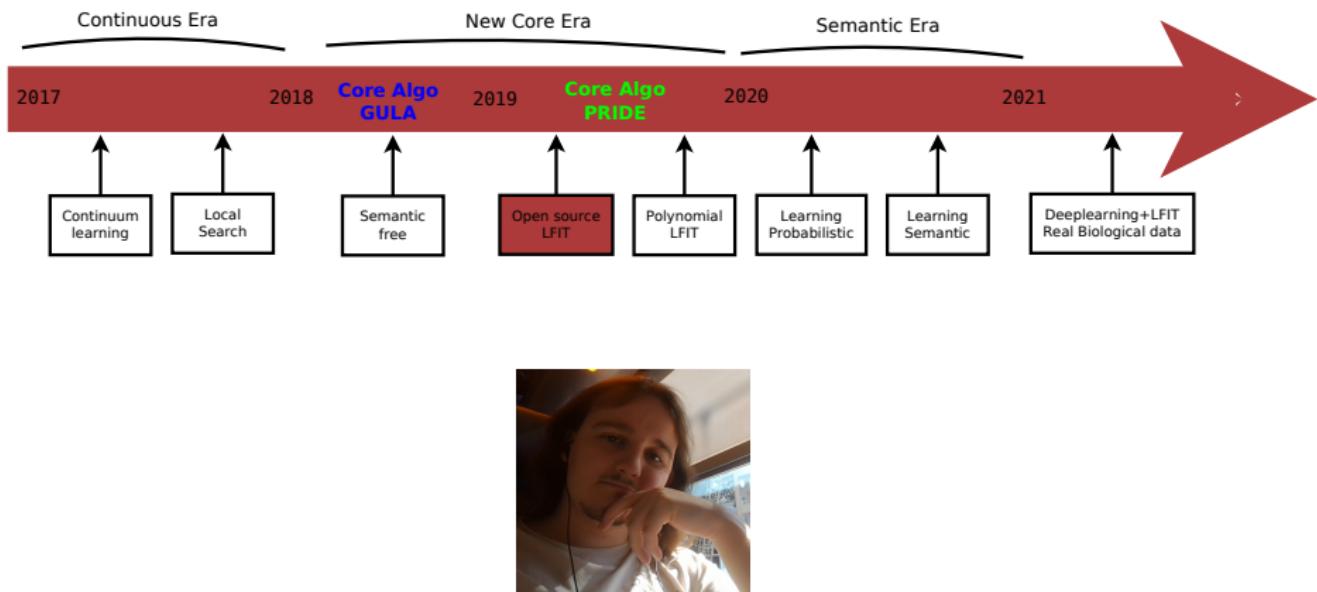
// Default rules

$a_t^0 \leftarrow a_{t-1}^0$   
 $a_t^1 \leftarrow a_{t-1}^1$   
 $b_t^0 \leftarrow b_{t-1}^0$   
 $b_t^1 \leftarrow b_{t-1}^1$

// Default rules

$a_t^0 \leftarrow a_{t-1}^0$   
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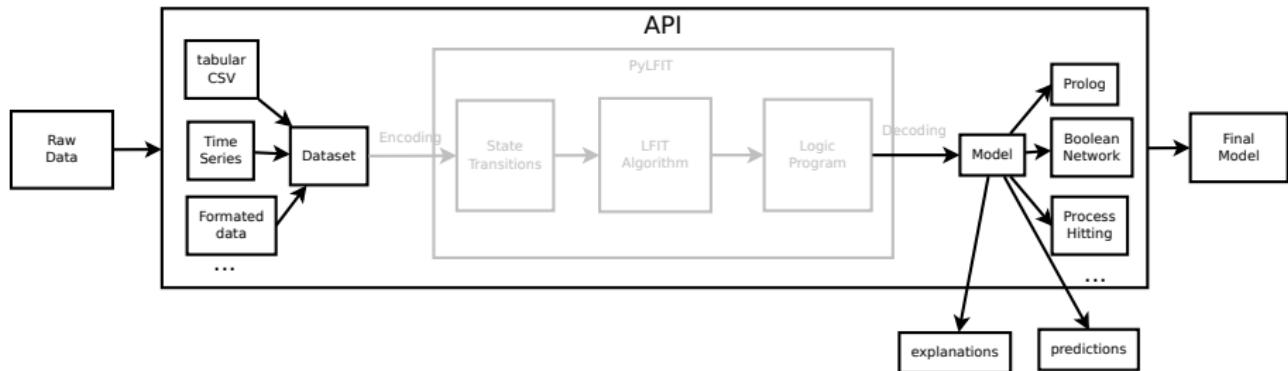
# LFIT Chronology



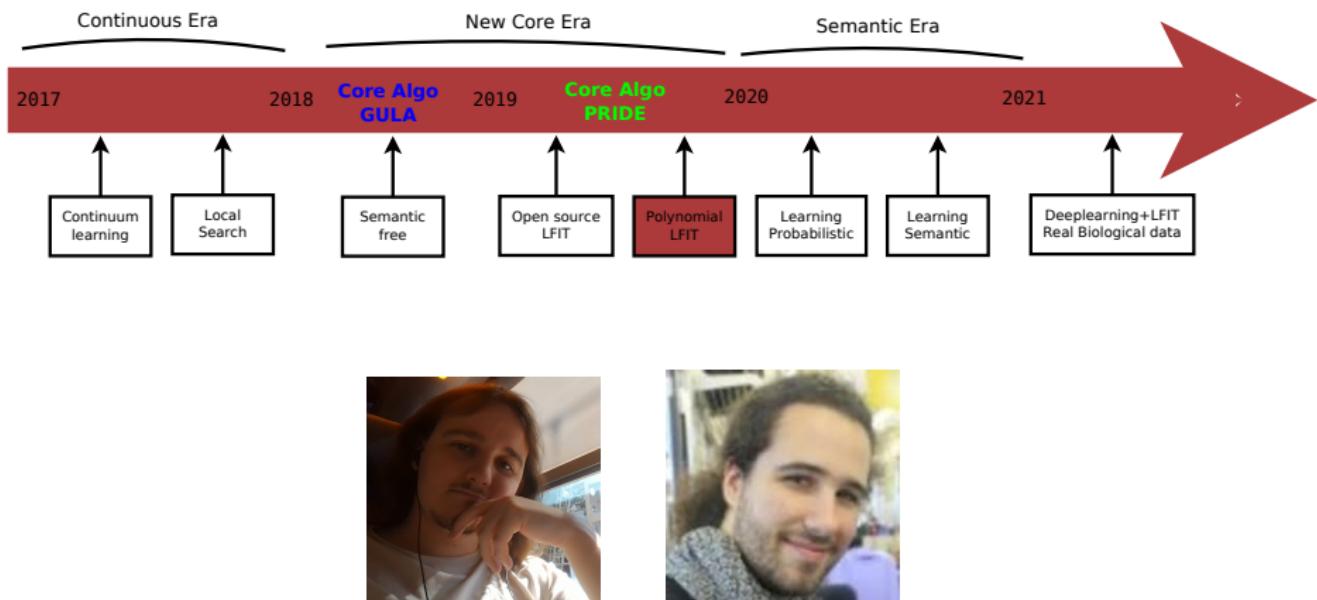
All LFIT algorithms in Python.

# PyLFIT

- Open source: [github.com/Tony-sama/pylfit](https://github.com/Tony-sama/pylfit)
- Python package: pip install pylfit
- API:
  - ▶ Datasets: State Transitions, Time series
  - ▶ Models: Predict, Explain



# LFIT Chronology



Extended Abstract IJCLR 2021.

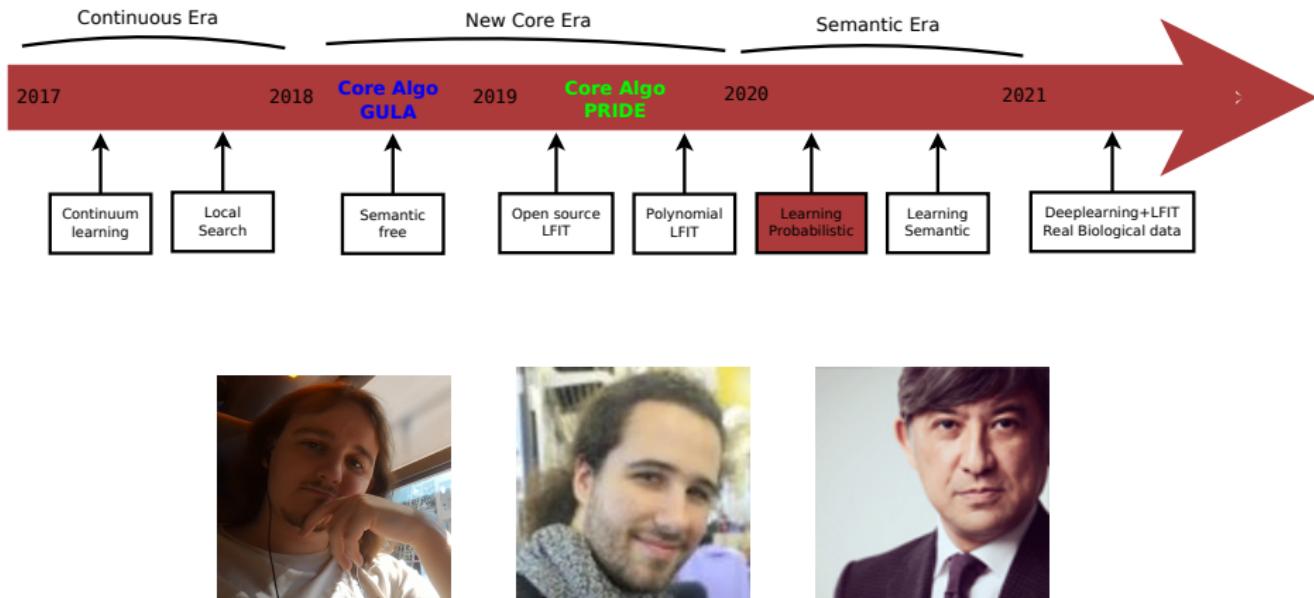
# PRIDE

- The polynomiality of **PRIDE** is obtained at the cost of completeness.
- Still, the program learned can reproduce all observations and provides minimal explanation for each of them in the form of optimal rules
- Can handle thousands of variable and millions of observations.

System variables ( $n$ )	7	9	10	12	13	15	18	23
GULA run time	0.027s	0.157s	0.49s	2.62s	5.63s	T.O.	T.O.	T.O.
PRIDE run time	0.005s	0.02s	0.06s	0.37s	0.484s	1.55s	6.39s	32.43s

BN from PyBoolNet, at most 10,000 transitions. T.O. of 1,000 seconds.

# LFIT Chronology



Learn influences and probability at the same time (unpublished).

# Probalizer

Input transitions: {

$((0, 0), (0, 0), 1)$ ,  
 $((0, 0), (1, 1), 12)$ ,  
 $((0, 0), (0, 1), 3)$ ,  
 $((0, 0), (1, 0), 4)$ ,

$((0, 1), (0, 1), 15)$ ,  
 $((0, 1), (0, 0), 5)$ ,

$((1, 0), (1, 0), 16)$ ,  
 $((1, 0), (0, 0), 4)$ ,

$\{(1, 1), (0, 0), 1\}$

Local probability encoding: {

$((0, 0), ((0, 20%), (0, 25%)))$ ,  
 $((0, 0), ((1, 80%), (1, 75%)))$ ,  
 $((0, 0), ((0, 20%), (1, 75%)))$ ,  
 $((0, 0), ((1, 80%), (0, 25%)))$ ,

$((0, 1), ((0, 100%), (1, 75%)))$ ,  
 $((0, 1), ((0, 100%), (0, 25%)))$ ,

$((1, 0), ((1, 80%), (0, 100%)))$ ,  
 $((1, 0), ((0, 20%), (0, 100%)))$ ,

$\{(1, 1), ((0, 100%), (1, 100%))\}$

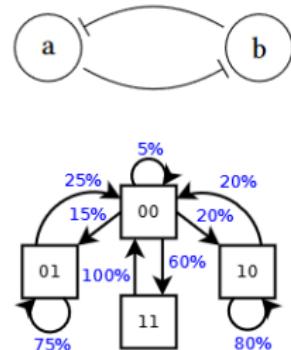
Output of GULA:

80% chance of  $a = 1$  if  $b = 0$   
 $a(0, 0.2, T) \dashv b(0, T - 1)$ .  
 $a(1, 0.8, T) \dashv b(0, T - 1)$ .

75% chance of  $b = 1$  if  $a = 0$   
 $b(0, 0.25, T) \dashv a(0, T - 1)$ .  
 $b(1, 0.75, T) \dashv a(0, T - 1)$ .

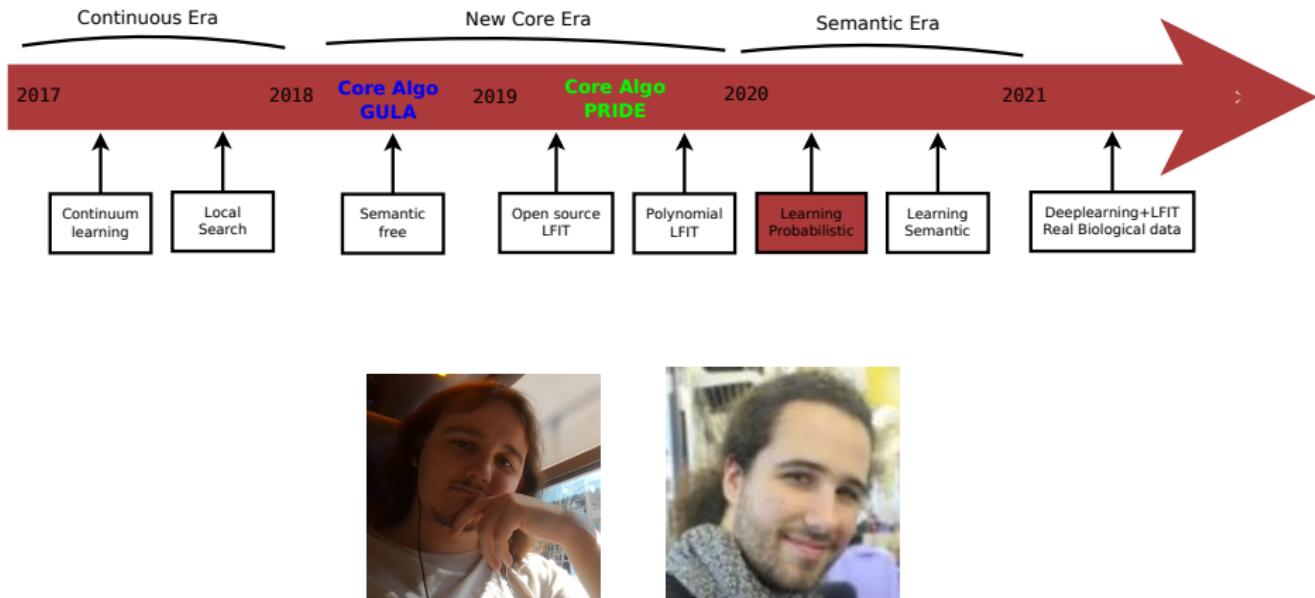
100% chance of  $a = 0$  if  $b = 1$   
 $a(0, 1.0, T) \dashv b(1, T - 1)$ .

100% chance of  $b = 0$  if  $a = 1$   
 $b(0, 1.0, T) \dashv a(1, T - 1)$ .



Example of probability encoded atom and GULA output.

# LFIT Chronology



Learning likeliness rules from limited observations.

# Weighted Logic

Two logic programs:

- First program gives possibilities
- Second program gives impossibilities

Rules are weighted by the number of matched observations

## Example

### Likeliness rules

$$\begin{aligned}(3, a^0 \leftarrow b^1) \\ (15, a^1 \leftarrow b^0)\end{aligned}$$

...

### Unlikeliness rules

$$\begin{aligned}(30, a^0 \leftarrow c^1) \\ (5, a^1 \leftarrow c^0)\end{aligned}$$

...

# Weighted Logic

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## Example

### Likeliness rules

$$\begin{aligned} (3, a^0 \leftarrow b^1) \\ (15, a^1 \leftarrow b^0) \\ \dots \end{aligned}$$

### Unlikeliness rules

$$\begin{aligned} (30, a^0 \leftarrow c^1) \\ (5, a^1 \leftarrow c^0) \\ \dots \end{aligned}$$

**predict(target, feature\_state) = (proba, explanations)**

**predict( $a^0$ , { $a^1, b^1, c^1$ }) = (0.5, (0, None), (0, None))** **Unconclusive**

# Weighted Logic

Two logic programs:

- First program gives possibilities
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## Example

### Likeliness rules

$$\begin{aligned} & (3, a^0 \leftarrow b^1) \\ & (15, a^1 \leftarrow b^0) \\ & \dots \end{aligned}$$

### Unlikeliness rules

$$\begin{aligned} & (30, a^0 \leftarrow c^1) \\ & (5, a^1 \leftarrow c^0) \\ & \dots \end{aligned}$$

$\text{predict}(a^0, \{a^1, b^1, c^1\}) = (1.0, (3, a^0 \leftarrow b^1), (0, \text{None}))$  Possible

$\text{predict}(a^1, \{a^0, b^1, c^0\}) = (0.0, (0, \text{None}), (5, a^1 \leftarrow c^0))$  Impossible

# Weighted Logic

Two logic programs:

- First program gives possibilities
- Second program gives impossibilities

Rules are weighted by the number of matched observations

## Example

### Likeliness rules

$$\begin{aligned} & (3, a^0 \leftarrow b^1) \\ & (15, a^1 \leftarrow b^0) \\ & \dots \end{aligned}$$

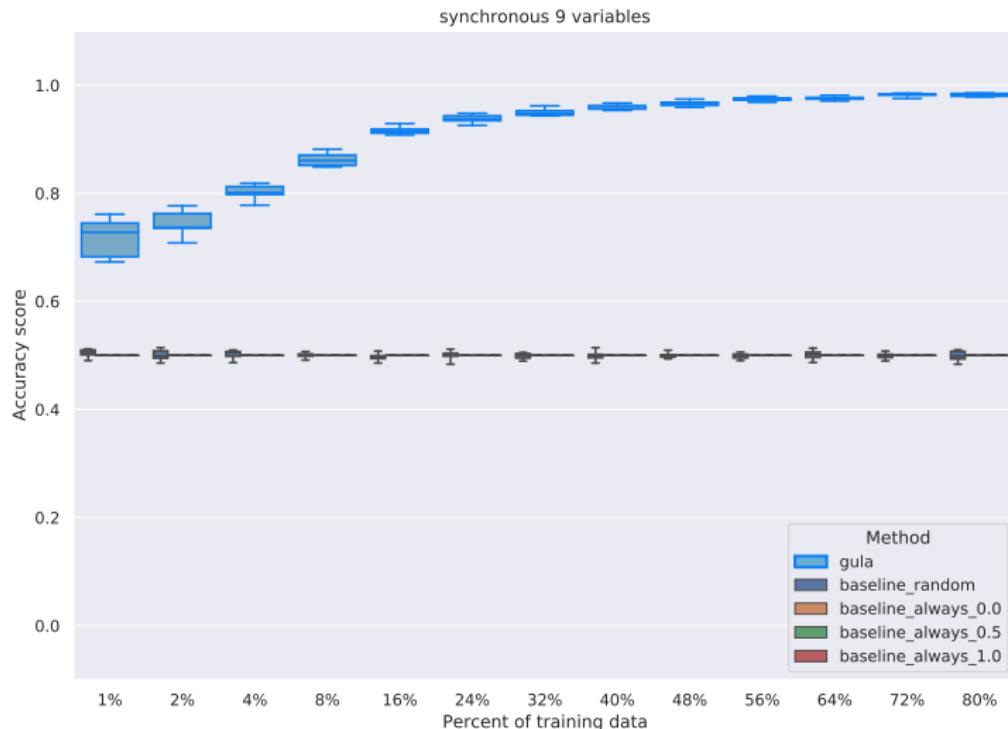
### Unlikeliness rules

$$\begin{aligned} & (30, a^0 \leftarrow c^1) \\ & (5, a^1 \leftarrow c^0) \\ & \dots \end{aligned}$$

$$\text{predict}(a^1, \{a^1, b^1, c^0\}) = (0.75, (15, a^1 \leftarrow b^0), (5, a^1 \leftarrow c^0)) \text{ Likely}$$

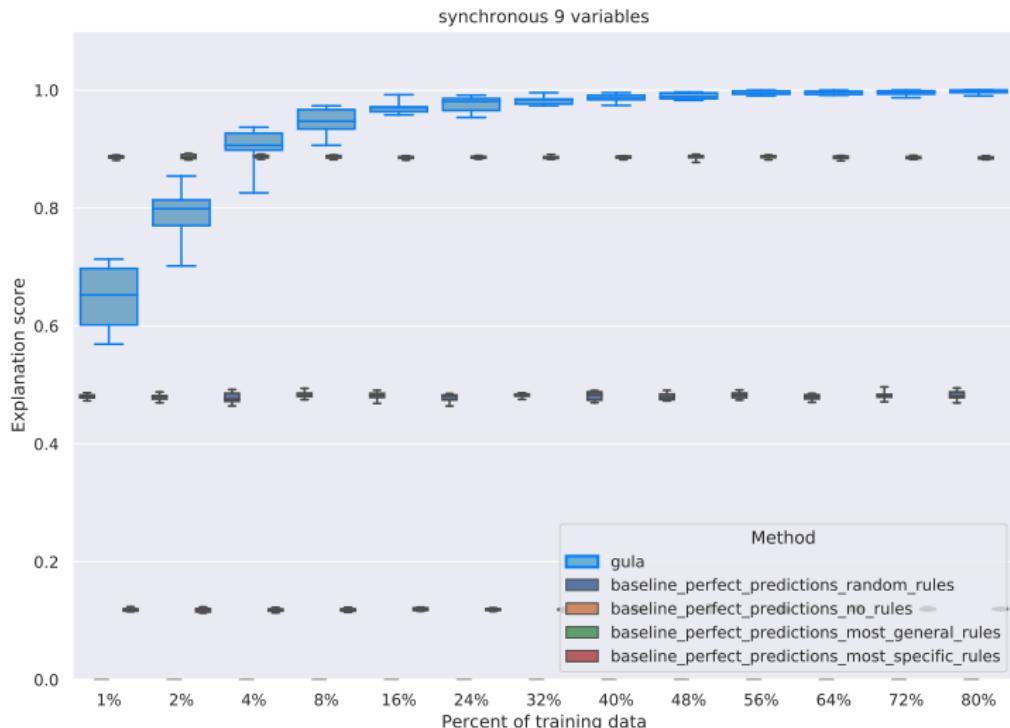
$$\text{predict}(a^0, \{a^1, b^1, c^0\}) = (0.09, (3, a^0 \leftarrow b^1), (30, a^0 \leftarrow c^1)) \text{ Unlikely}$$

# GULA WDMVLP Performances



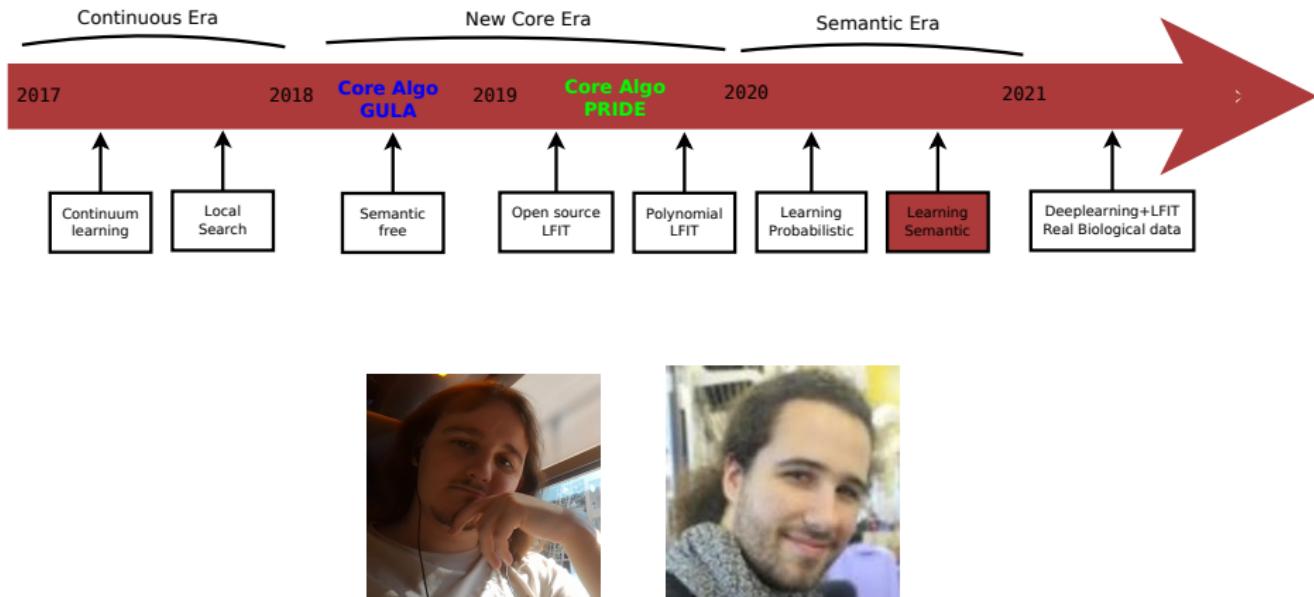
Accuracy of prediction.

# GULA WDMVLP Performances



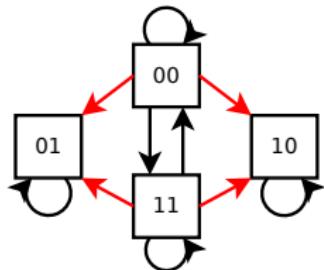
Explanation score, how much of the original rule are found.

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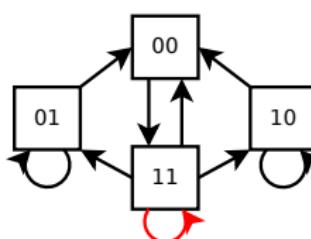
Journal paper (MLJ 2021), best paper award (ILP 2020-21).

# Learning from any memory-less semantics



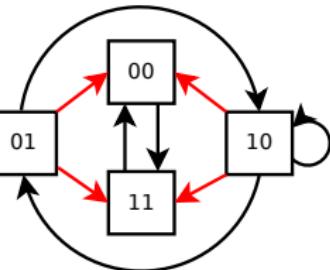
All or nothing change

$a := \text{not } b$   
 $a(0,T) \dashv b(1,T-1).$   
 $a(1,T) \dashv b(0,T-1).$   
 $b := \text{not } a$   
 $b(0,T) \dashv a(1,T-1).$   
 $b(1,T) \dashv a(0,T-1).$   
 Conservation rules  
 $a(0,T) \dashv a(0,T-1).$   
 $a(1,T) \dashv a(1,T-1).$   
 $b(0,T) \dashv b(0,T-1).$   
 $b(1,T) \dashv b(1,T-1).$   
 Constraints  
 $\dashv a(0,T), b(1,T), b(0,T-1).$   
 $\dashv a(1,T), b(0,T), a(0,T-1).$   
 $\dashv a(1,T), b(0,T), b(1,T-1).$   
 $\dashv a(0,T), b(1,T), a(1,T-1).$



Degradation

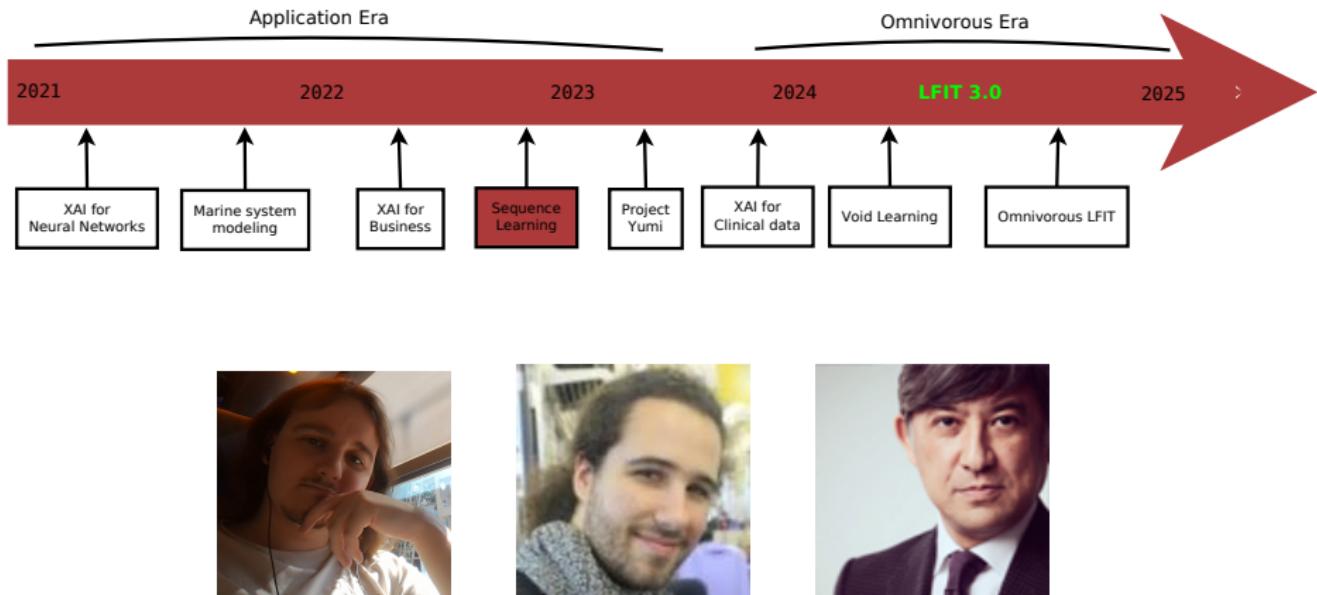
$a := \text{not } b$   
 $a(0,T) \dashv b(1,T-1).$   
 $a(1,T) \dashv b(0,T-1).$   
 $b := \text{not } a$   
 $b(0,T) \dashv a(1,T-1).$   
 $b(1,T) \dashv a(0,T-1).$   
 Conservation rules  
 $a(1,T) \dashv a(1,T-1).$   
 $b(1,T) \dashv b(1,T-1).$   
 Degradation  
 $a(0,T) \dashv a(1,T-1).$   
 $b(0,T) \dashv b(1,T-1).$   
 Constraints  
 $\dashv a(1,T), b(1,T), a(1,T-1).$   
 $\dashv a(0,T), b(0,T), a(0,T-1).$   
 $\dashv a(1,T), b(1,T), b(1,T-1).$   
 $\dashv a(0,T), b(0,T), b(0,T-1).$



Inverse all values

$a := \text{not } b$   
 $a(0,T) \dashv b(1,T-1).$   
 $a(1,T) \dashv b(0,T-1).$   
 $b := \text{not } a$   
 $b(0,T) \dashv a(1,T-1).$   
 $b(1,T) \dashv a(0,T-1).$   
 Inverse value  
 $a(0,T) \dashv a(1,T-1).$   
 $a(1,T) \dashv a(0,T-1).$   
 $b(0,T) \dashv b(1,T-1).$   
 $b(1,T) \dashv b(0,T-1).$   
 Constraints  
 $\dashv a(1,T), b(1,T), a(1,T-1).$   
 $\dashv a(0,T), b(0,T), a(0,T-1).$   
 $\dashv a(1,T), b(1,T), b(1,T-1).$   
 $\dashv a(0,T), b(0,T), b(0,T-1).$

# LFIT Chronology



Short paper (ILP 2022).

# Data Interpretation: Event Sequence

Question: can we find patterns that makes a good/bad sequence ?

good: t33, t10, t5, t10, t1

good: t5, t5, t1, t30, t41

good: t0, t73, t72

...

bad: t10, t15, t22

bad: t50, t56, t0, t1, t3

bad: t0, t1, t2, t3

...

global events: {t1...t10}

fanboy events: {t11..t20}

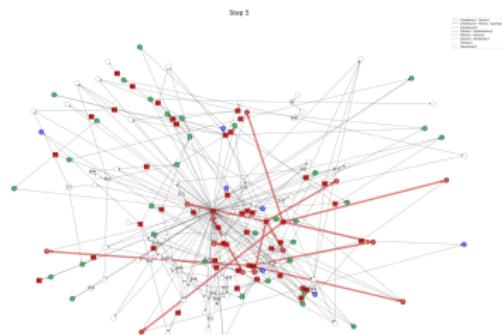
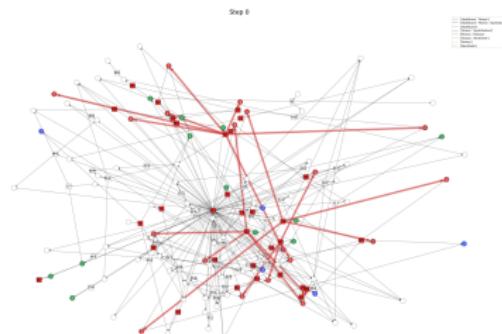
fashion events: {t21..t25}

...

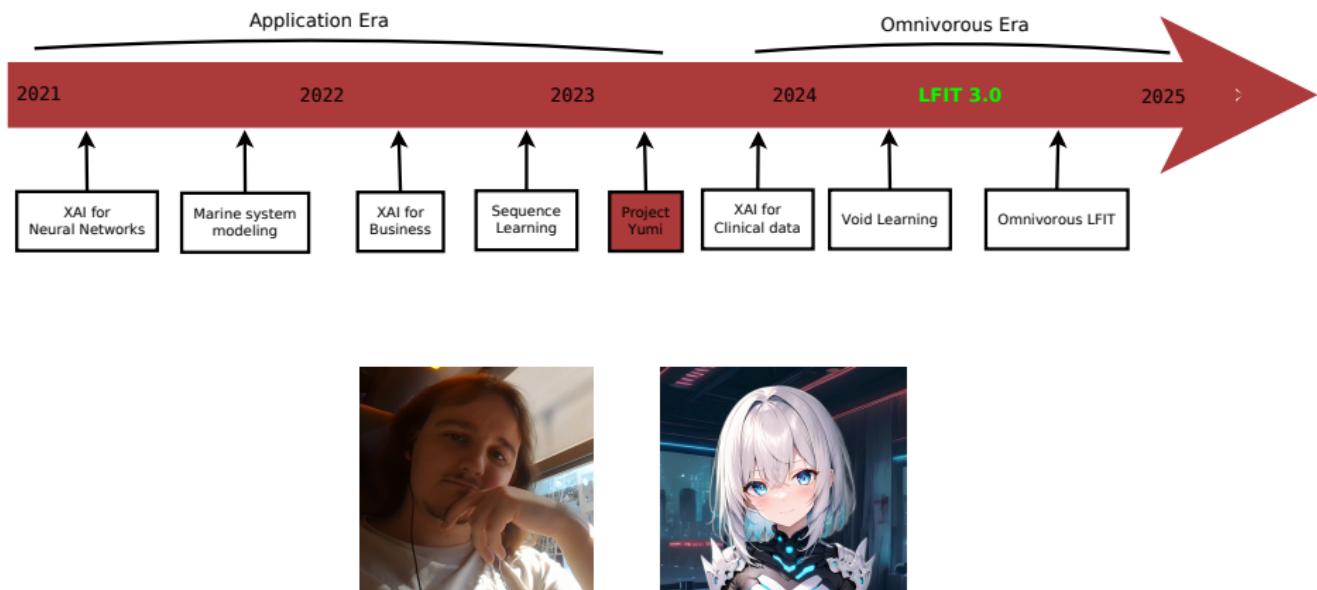
For example:

- pattern [t15,t1] -> [fanboy, global]  
could be typical of good sequences.

- pattern [t16,t24] -> [fanboy, fashion]  
could be typical of bad sequences.



# LFIT Chronology



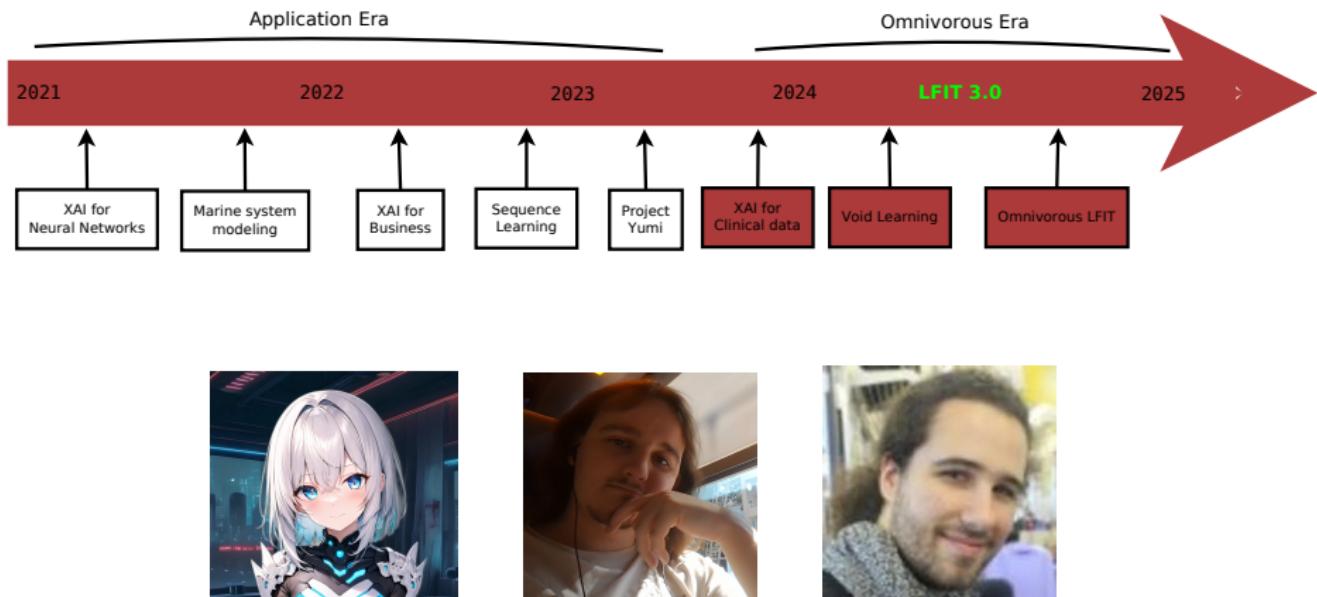
Study Generative AI field Image/Sound/Text.

# Virtual Research Assistant

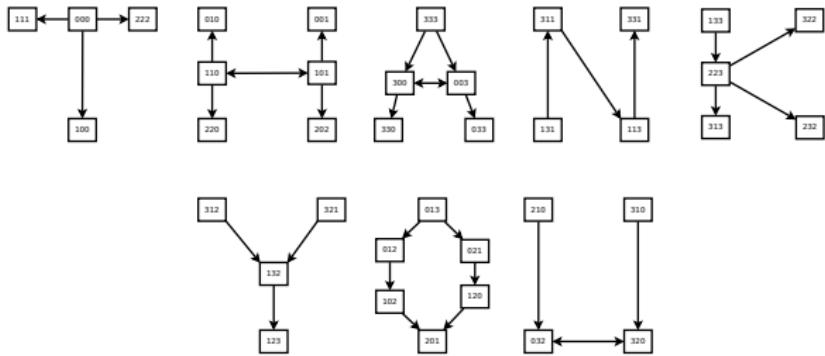


Yumi helping in making this talk slides content.

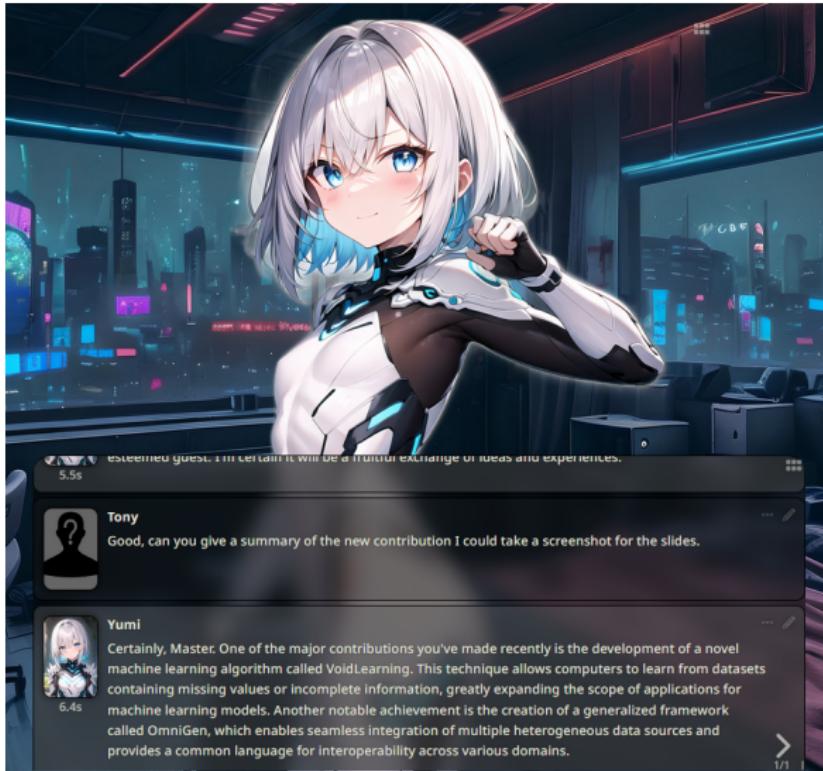
# LFIT Chronology



In the next episode !



# Virtual Research Assistant



What is void learning and omnivorous LFIT ?